

# Cryptography

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Exercise Sheet 7  
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**Exercise 1.**

Consider the following binary block code  $C \subseteq \mathbb{Z}_2^7$ :

$$C := \{(c_1, \dots, c_7) \in \mathbb{Z}_2^7 \mid c_1 + c_2 + c_3 + c_5 = 0, c_1 + c_2 + c_4 + c_6 = 0, c_2 + c_3 + c_4 + c_7 = 0\}.$$

Show that  $C$  is 1-error detecting perfect code.

**Exercise 2.**

Find the ISIN-*control character* of the share of the following stock companies:

- c) Volkswagen: DE000766400□,
- d) Peugeot: FR000012150□ and
- e) Toyota: JP363340000□.

**Exercise 3.**

Consider the following ISBN10 parity code of length 10 to the base 11 with weights  $w_i := 11 - i$ ,  $i = 1, \dots, 10$ .

- a) Find the *control character* of the ISBN10 code 360893823□ of the 6th. edition of the novel "*The Lord of the Rings*" in the publisher Klett Cotta.
- b) Show that the following equation can also be used to find the the *control character*  $c_{10}$  of ISBN10 codes:  $1 \cdot c_1 + \dots + 9 \cdot c_9 \equiv c_{10} \pmod{11}$ .
- c) Show that the exchange of any two position of an ISBN10 code will be detected.