$\begin{array}{c} \text{Convection in} \\ \text{low rotating} \\ \text{spherical shells} \\ 1/42 \end{array}$ 

## B. Futterer and C. Egbers

Introduction

Motivation Physical Basics

3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison Instabilities and transition in the GeoFlow experiment on ISS: Quasi-stationary and chaotic convection in low rotating spherical shells

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Convection in low rotating spherical shells 2/42

## B. Futterer and C. Egbers

#### Introduction

Motivation Physical Basics

3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

### Introduction

Motivation Physical Basics

### **2** 3D numerical simulation

Borders of low rotation Low rotation: transition to higher *Ra* Low rotation: transition to higher *Ta* 

## **3** Summary, Outlook and Appendices

## Outline

Convection in low rotating spherical shells 3/42

B. Futterer and C. Egbers

#### Introduction

#### Motivation

Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

# Spherical Rayleigh-Bénard convection in self-gravitating force field, superposition of rotation

### radial gravity force (dielectrophoretic)

- I. Yavorskaya, N. Fomina, Y. Belyaev, A simulation of central-symmetry convection in microgravity conditions, Acta Astronaut. 11 (1984), 179–183
- J. Hart, G. Glatzmaier, J. Toomre Space-laboratory experiments and numerical simulations of thermal convection in a rotating hemispherical shell with radial gravity, J. Fluid Mech. 173 (1986), 512–544
- spherical shell convection
  - H.F. Busse, Patterns of convection in spherical shells, J. Fluid Mech. 72 (1975), 67–85

### convection in rotating shells (recent)

- F.H. Busse, *Convective flows in rapidly rotating spheres and their dynamo action,* Phys. Fluids 14 (2002), 1301–1313
- R. Simitev & F.H. Busse, Patterns of convection in rotating spherical shells, New J. of Physics 5 (2003), 97.1–97.20
- R. Simitev & F.H. Busse, Prandtl-number dependence of convection-driven dynamos in rotating spherical shells, J. Fluid Mech. 532 (2005), 365–388
- N. Gillet, D. Brito, D. Jault, H.-C. Nataf, Experimental and numerical studies of convection in a rapidly rotating spherical shell, J. Fluid Mech. 580 (2007), 83–121
- F. Garcia, J. Sanchez, M. Net, Antisymmetric polar modes of thermal convection in rotating spherical fluid shells at high Taylor numbers, Phys. Rev Lett. 101 (2008), 365–388



Earth's interior's scaled to spherical shells



Sketch of experimental shell system

Convection in low rotating spherical shells 4/42

B. Futterer and C. Egbers

#### Introduction

#### Motivation

Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

## Objectives of GeoFlow **experiment**:

spherical Rayleigh-Bénard convection in self-gravitating force field, superposition of rotation

 radial gravity force by high voltage potential between inner and outer spherical shells

(dielectrophoretic effect in microgravity environment on ISS)

- fully spherical shell with radius ratio of  $\eta = 0.5$ , filled with dielectric fluid of  $Pr \approx 65$
- spherical shell convection for non-rotating case
- convection in rotating spherical shells
- Rayleigh number  $Ra_{centr} \approx 2 \cdot 10^5 \ (Ra \sim \Delta T)$ , Taylor number  $Ta \approx 10^7 \ (Ta \sim f)$
- non-magnetic experiment

### characterization

- flow patterns of convection for non-rotating and rotating spherical shells
- identification of stability of co-existing modes (Ta = 0)
- identification of travelling waves (*Ta* low)
- change of sign for drift velocities (*Ta* intermediate)
- up to columnar cells at the tangent cylinder (*Ta* high)

Convection in low rotating spherical shells 5/42

B. Futterer and C. Egbers

Introduction

Motivation

Physical Basics

3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison Non-dimensional Boussinesq equations for dielectric convection in spherical shells

 $\nabla\cdot \bm{U}=0$ 

$$Pr^{-1}\left[\frac{\partial \mathbf{U}}{\partial t} + (\mathbf{U} \cdot \nabla)\mathbf{U}\right] = -Pr^{-1}\nabla p + \nabla^2 \mathbf{U} + Ra_{centr} \cdot \frac{\eta^2}{(1-\eta)^2} \cdot \frac{1}{r^5} T \,\hat{\mathbf{e}}_r$$
$$-\sqrt{Ta} \,\hat{\mathbf{e}}_z \times \mathbf{U} + \widetilde{Ra} T \, r \sin \theta \hat{\mathbf{e}}_{eq}$$

 $\frac{\partial T}{\partial t} + \mathbf{U} \cdot \nabla T = \nabla^2 T$ 

no-slip boundary conditions for velocity **U**, temperature fixed  $T(\eta) = 1$ , T(1) = 0; rotating reference frame, scaled to outer spherical radius

### Parameters

radius ratio

Prandtl number

Rayleigh number

Taylor number

additional factor

$$Pr = \frac{\nu}{\kappa}$$

 $\eta = \frac{r_i}{r_o}$ 

$$Ra_{centr} = rac{2\epsilon_0\epsilon_r\gamma}{
ho\nu\kappa} V_{
m rms}^2 \,\Delta T$$

$$Ta = \left(\frac{2\Omega r_o^2}{\nu}\right)^2$$

 $\widetilde{Ra} = \frac{\alpha \Delta T}{4}$  Ta Pr



Convection in	Experimental constraints								
low rotating spherical shells						GeoFlow	outer	mantle	
6/42							core		
	gap	$r_o - r_i[mm]$	13.5	$\rightarrow$	$\eta$	0.5	0.37	0.55	
B. Futterer									
and C. Egbers	viscosity	$ u[m/s^2]$	$5 \cdot 10^{-6}$	$\rightarrow$	Pr	64.64	0.1-	$\infty$ ,	
Introduction							1.0		
Mativation								F(T,z)	
Physical Basics	voltage	V [kV]	10	۱				- ( - , - )	
T Hysical Dasies	tonon another		10 < 10		Ra <sub>cent</sub>	$_r \leq 1.4 \cdot 10^5$	$> 10^{29}$	$10^{6}-10^{8}$	
3D numerical	temperature	$\Delta I[K]$	$\leq 10$	J					
simulation									
Borders of low	rotation	f[Hz]	$\leq 2$	$\rightarrow$	Ta	$\leq 1.3\cdot 10^7$	10 <sup>30</sup>	<< 1	

### Spectral method for numerical simulation

- decomposition of primary variables into poloidal and toroidal parts
- decomposition of these into Chebyshev polynomials and spherical harmonics
- solving equations for spectral coefficients  $e(r, \theta, \varphi, t) = \sum_{m=0}^{M} \sum_{\ell=m'}^{L} \sum_{k=1}^{K} e_{k\ell m} T_{k-1}(x) P_{\ell}^{|m|}(\cos \theta) e^{im\phi}$
- truncation with (K,L,M)=(30,60,20)
- R. Hollerbach, A spectral solution of the magneto-convection equations in spherical geometry, Int. J. Numer. Meth. Fluids 32 (2000), 773–797
- global variables

$$Nu = -r^2 \frac{r_o - r_i}{r_i r_o} \frac{\partial T}{\partial r} \rightarrow Nu_i = -\frac{r_i}{r_o} (r_o - r_i) \frac{\partial T}{\partial r}$$
  

$$E_{kin} = 0.5 \cdot \int (u_r^2 + u_\theta^2 + u_\phi^2) \cdot r^2 \sin(\theta) \, dr \, d\theta \, d\phi$$

Summary, Outlook and Appendices

Low rotation:

Low rotation: transition to higher

Ra

Ta

transition to higher

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

#### Convection in low rotating spherical shells 7/42

B. Futterer and C. Egbers

#### Introduction

Motivation

Physical Basics

## 3D numerical simulation

### Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

### Flow modes of the lower limit: non-rotating case Ta = 0



### Patterns of convection:

Visualization of temperature field in radial direction, red color corresponds to hot up-flow and blue color to cold discharge.

Co-existing modes (K. Bergemann, L. Tuckerman, F. Feudel, *GeoFlow: On symmetry-breaking bifurcations of heated spherical shell convection*, J. Phys.: Conf. Ser. **137** (2008), 012027 (4pp)).



### Patterns of convection:

apparatus

single images

Experimental/ numerical comparison

Parameter regimes:

Parameter regimes: constructed images

Visualization of temperature field, view at the top of the sphere, i.e. the middle of the image is the 'polar' region.

Increase of mode number (V. Travnikov, R. Hollerbach, C. Egbers, *The GEOFLOW experiment on ISS. Part II: Numerical simulation*, Adv. Space Res. 32 (2003), 181–189).

#### Convection in low rotating spherical shells 9/42

## B. Futterer and C. Egbers

#### Introduction

Motivation

Physical Basics

## 3D numerical simulation

Borders of low rotation

#### Low rotation: transition to higher *Ra*

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

### Dynamics of low rotating spherical shell convection I



### Patterns of convection:

Visualization of radial velocity field, red color corresponds to positive and blue color to negative direction of flow.

Modes as in the non-rotating regime.



numerical comparison



## B. Futterer and C. Egbers

#### Introduction

Motivation

Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

### Dynamics of low rotating spherical shell convection II



Space time plots of azimuthal velocity component: change of sign for drift velocity, also predicted by means of stability analysis (Travnikov et. al, 2003).

#### Convection in low rotating spherical shells 12/42

#### B. Futterer and C. Egbers

Ra

Ta

physical basics

analysis, path-following Experimental apparatus

Time series, linear

Parameter regimes: single images Parameter regimes: Example:  $Ra = 3 \cdot 10^3$ 

#### param. Introduction $2\cdot 10^2$ $2\cdot 10^3$ $8\cdot10^3$ Ta Motivation Physical Basics 3D numerical simulation Borders of low rotation Low rotation: transition to higher Low rotation: transition to higher Nu, E<sub>kin</sub> irregular const. const. Summary, coeff. irregular periodic quasi-periodic Outlook and Pattern of convection by visualization of temperature field in radial direction with **Appendices** State of the art,

view from side. Isolines demonstrate character of the pattern. Dark shading shows hot up-flow.

constructed images Experimental/ numerical comparison Convection in low rotating spherical shells 13/42

B. Futterer and C. Egbers

Introduction

Physical Basics

Borders of low rotation

Low rotation:

Low rotation: transition to higher

Summary, Outlook and

**Appendices** 

State of the art, physical basics Time series, linear

path-following Experimental apparatus

analysis,

Ra

Ta

transition to higher

3D numerical simulation

Motivation

### Summary

- GeoFlow
  - spherical Rayleigh-Bénard convection experiment in self-gravitating force field
  - microgravity environment of COLUMBUS on ISS
  - superposition of rotation
  - rotating regimes from Ta = 0 via low, intermediate up to rapid
- dynamics for low rotating regime
  - comparable to Ta = 0:
    - coexisting of several modes (axisymmetric, cubic, pentagonal)
    - transition from quasi-stationary to irregular flow with remnant tetrahedral symmetry
  - intermediate regime
    - change of sign for drift
    - prograde  $\rightarrow$  retrograde

### Outlook

• comparison with experimental data

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison Convection in low rotating spherical shells 14/42

B. Futterer and C. Egbers

#### Introduction

Motivation

Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

### State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

### State of the art:

spherical Rayleigh-Bénard convection in self-gravitating force field, superposition of rotation

- radial gravity force by dielectrophoretic effect in microgravity environment
  - Yavorskaya et al. A simulation of central-symmetry convection in microgravity conditions. Acta Astronautica 11 (1984), 179–183
  - Hart et al. Space-laboratory experiments and numerical simulations of thermal convection in a rotating hemispherical shell with radial gravity. J. Fluid Mech. 173 (1986), 512–544
- spherical shell convection for non-rotating case
  - H.F. Busse. Patterns of convection in spherical shells. J. Fluid Mech. 72 (1975), 67-85
- convection in rotating spherical shells
  - A. Tilgner & F.H. Busse. *Finite-amplitude convection in rotating spherical shells.* J. Fluid Mech. 332 (1997), 359–376
  - F.H. Busse. *Convective flows in rapidly rotating spheres and their dynamo action.* Phys. Fluids 14 (2002), 1301–1313
  - R. Simitev & F.H. Busse. *Patterns of convection in rotating spherical shells.* New J. of Physics 5 (2003), 97.1–97.20
  - R. Simitev & F.H. Busse. *Prandtl-number dependence of convection-driven dynamos in rotating spherical shells.* J. Fluid Mech. 532 (2005), 365–388
  - N. Gillet, D. Brito, D. Jault, H.-C. Nataf. *Experimental and numerical studies of convection in a rapidly rotating spherical shell.* J. Fluid Mech. 580 (2007), 83–121
  - F. Garcia, J. Sanchez, M. Net. Antisymmetric polar modes of thermal convection in rotating spherical fluid shells at high Taylor numbers. Phys. Rev Lett. 101 (2008), 365–388

Convection in low rotating spherical shells 15/42

B. Futterer and C. Egbers

#### Introduction

Motivation

Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

### State of the art: spherical Rayleigh-Bénard convection in self-gravitating force field, superposition of rotation

• radial gravity force by dielectrophoretic effect in microgravity environment

#### theoretical discussion of central-symmetry convection in spherical layers under dielectrophoretic force in microgravity conditions

- $\mu = 0.5 \ldots 0.9$ ,  $Pr = 15 \ldots 1020$ ,  $Ra pprox 10^7$ , Ta = 0
- Spacelab 3 experiment for thermally driven circulations within rotating hemispherical shell  $\mu = 0.73$ , Pr = 8.4,  $Ra \approx 10^6$ ,  $Ta = 6 \cdot 10^5$
- spherical shell convection for non-rotating case
  - pattern of motion in convectively unstable system with spherical geometry I = 4 is responsible for the onset of convection
- convection in rotating spherical shells
  - drifting waves, time-dependent convection, heat transport  $\mu = 0.4$ ,  $Pr = 0.01 \dots 10$ ,  $Ra \approx 3 \cdot 10^5$ ,  $Ta = 10^6$
  - Coriolis force, Rossby waves in centrifugally driven convection in rotating annulus, convection in rotating self-gravitating spherical shells
    - $\mu=$  0.4,  $\textit{Pr}=0.025\ldots1$ ,  $\textit{Ra}pprox10^{6}$ ,  $\textit{Ta}pprox10^{4}$
  - patterns of convection in internally heated convection, amplitude vascillations and spatial modulations of convective columns

$$\mu=$$
 0.4,  ${\it Pr}=$  0  $\ldots$  100,  ${\it Ra}pprox$  10 $^{6}$ ,  ${\it Ta}pprox$  10 $^{4}$ 

- low Pr promote dynamo action, high Pr number fluids influence on dynamo action  $\mu = 0.4$ ,  $Pr = 0.025 \dots 20$ ,  $Ra \approx 10^6$ ,  $Ta \approx 10^5$
- experiment with cylinder in the sphere  $\mu = 0.36$ , Pr = 7,  $Ra \approx 10^6$ ,  $Ta \approx 10^6$
- onset of convection  $\mu = 0.4, Pr = 0.01, Ra \approx 10^6, Ta \approx 10^{11}$

Convection in low rotating spherical shells 16/42

#### **B**. Futterer and C. Egbers

#### Introduction

Motivation

Physical Basics

#### **3D** numerical simulation

Borders of low rotation

Low rotation: transition to higher Ra

Low rotation: transition to higher Ta

#### Summary, Outlook and **Appendices**

#### State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

## Coulomb force

- charged particle in electric field **E**
- $F_C(r) = q E$
- much stronger than dielectrophoretic force
- suppressed by using high-frequency AC voltage  $(T_{el} \ll \tau)$ 
  - $\tau$  relaxation time of free particle)

## Dielectrophoretic force

- due to polarisation of medium in electric fields (local dipoles)
- $\mathbf{F}_{\mathbf{D}}(\mathbf{r}) = \frac{1}{2}\mathbf{E}^{2}(\mathbf{r})\nabla\epsilon$
- acting as a ponderomotive force only in geometrically inhomogeneous field
- resulting movement only for dieletric inhomogenous media
- depends on gradient of **E**, not sign
- spherical geometry:  $F_D(r) \sim 1/r^5$
- acts as central force field (comparable to gravity)

### GeoFlow constraints

- spherical shell system is geometrically inhomogenous
- experimental fluid is dielectric homogenous



Homogeneous electric field:



Inhomogeneous electric field:

#### F.< -F., resulting force

Convection in low rotating spherical shells 17/42

B. Futterer and C. Egbers

#### Introduction

Motivation Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison Setting up high voltage  $\rightarrow$  acceleration due to dielectric force field

$$\mathbf{g}_{\mathbf{e}} = \frac{1}{2\rho} \epsilon \epsilon_r \nabla |\mathbf{E}|^2 \quad \text{with} \quad \mathbf{E} = \frac{1}{r^2} \frac{r_i r_o}{r_o - r_i} V_0 \sin(\omega t) \hat{\mathbf{e}}_r$$

$$g_e = \frac{2\epsilon_0\epsilon_r}{\rho} \left(\frac{r_i r_o}{r_o - r_i}\right)^2 V_{rms}^2 \frac{1}{r^5}$$

 $\varepsilon_0$  - dielectric constant,  $\varepsilon_r$  - relative permittivity,  $\rho$  - density,  $V_{rms}$  - voltage GeoFlow specific values . . .

$$\epsilon_0 = 8.854 \cdot 10^{-12} \text{ As}/Vm, \quad \epsilon_r = 2.7,$$

 $ho=920~{
m kg/m^3},$ 

$$d = r_o - r_i = 27 mm - 13.5 mm = 13.5 mm$$
,

 $V_{rms} = 10 ~kV$  $ightarrow g_e|_{r_o} pprox 10^{-1} m/s^2$  compared to  $g pprox 10^1 m/s^2$ 

 $\rightarrow$  microgravity conditions required!

#### Convection in low rotating spherical shells 18/42

# Timeseries for identification of time-dependencies in numerical solutions: global variable of kinetic energy

## B. Futterer and C. Egbers

#### Introduction

Motivation

Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison



Convection in low rotating spherical shells 19/42

B. Futterer and C. Egbers

#### Introduction

Motivation

Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison Timeseries for identification of time-dependencies in numerical solutions: global variables of kinetic energy and Nusselt number, local variables of spectral coefficient:  $Ra_{centr} = 4 \cdot 10^3$ ,  $Ta = 5 \cdot 10^2$ 



Convection in low rotating spherical shells 20/42

B. Futterer and C. Egbers

#### Introduction

Motivation

Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

### History of simulation work for GeoFlow

- Stability analysis for both cases Ta = 0 (determination of onset of convection) and  $Ta \neq 0$  (influence of centrifugal force, modes of instabilities)
  - V. Travnikov, R. Hollerbach, C. Egbers, *The GEOFLOW experiment on ISS. Part II: Numerical simulation*, Adv. Space Res. 32 (2003), 181–189
  - V. Travnikov, *Thermische Konvektion im Kugelspalt unter radialem Kraftfeld*, Dissertation, Cuvillier Verlag Göttingen, 2004
- Bifurcation analysis (influence of different force fields in geo-/astrophysical framework)
  - P. Beltrame, V. Travnikov, M. Gellert, C. Egbers, *GEOFLOW: Simulation of convection in a spherical gap under central force field*, Nonlinear Processes in Geophysics, 13, 1-11
- Path following analysis (determination of stable and unstable solutions for stationary states for case Ta = 0)
  - K. Bergemann, L. Tuckerman, F. Feudel, *GeoFlow: On symmetry-breaking bifurcations of heated spherical shell convection*, J. Phys.: Conf. Ser. **137** (2008), 012027 (4pp)
- Direct numerical simulations (fluid flow and temperature field, calculation of interferograms)
  - M. Gellert, P. Beltrame, C. Egbers, The GeoFlow experiment spherical Rayleigh-Bénard convection under the influence of an artificial central force field, J. Phys.: Conf. Ser. 14 (2005), 157-161
  - B. Futterer, M. Gellert, Th. von Larcher, C. Egbers, Thermal Convection in rotating spherical shells: An experimental and numerical approach within GeoFlow, Acta Astronautica 62 (2008), 300–307
  - B. Futterer, R. Hollerbach, C. Egbers, *Geoflow: 3D numerical simulation of supercritical thermal convective states*, J. Phys.: Conf. Ser. **137** (2008), 012026 (5pp)

Convection in low rotating spherical shells 21/42

### Linear analysis for Ta = 0

B. Futterer and C. Egbers

#### Introduction

Motivation

Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison



critical Racentr for onset of convection independent on Pr

• larger  $\eta \rightarrow$  larger critical mode l

Source: V. Travnikov, C. Egbers, R. Hollerbach, *The GEOFLOW experiment on ISS. Part II: Numerical simulation*, Adv. Space Res. 32 (2003), 181–189 V. Travnikov: *Thermische Konvektion im Kugelspalt unter radialem Kraftfeld*, Dissertation, Cuvillier Verlag Göttingen, 2004 Convection in low rotating spherical shells 22/42

### Linear analysis for $Ta \neq 0$

B. Futterer and C. Egbers

#### Introduction

Motivation

Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison



- shape of stability curves nearly independent on Pr
- instability due to Hopf bifurcation
- for large *Ta*:  $Ra_{centr} \sim Ta^{2/3}$

[P.H. Roberts, *On the thermal instability of a rotating-fluid sphere containing heat sources*, Philos. Trans. R. Soc. London 263 (1968), 93-117]

drift velocity W changes sign (slows down or fastens rotation)

Source: Travnikov et al. (2003), Travnikov (2004)

#### Convection in low rotating spherical shells 23/42

#### B. Futterer and C. Egbers

#### Introduction

Motivation

Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

### Path-following analysis for stationary solutions at Ta = 0



- existence of multistability (axisymmetry, cubic, m = 5)
- sudden onset of chaos at Ra > 28000
- hysteresis behaviour of the chaotic branch resulting in frozen states with tetrahedral symmetry

Source: K. Bergemann, L. Tuckerman, F. Feudel, *GeoFlow: On symmetry-breaking bifurcations of heated spherical shell convection*, J. Phys.: Conf. Ser. **137** (2008), 012027 (4pp) K. Bergemann: *Konvektion im Kugelspalt: Numerische Untersuchung und Bifurkationsanalyse am Beispiel des GeoFlow-Experimentes*, Diplomarbeit, Universität Potsdam, 2008

#### Convection in low rotating spherical shells 24/42

## B. Futterer and C. Egbers

#### Introduction

Motivation

Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

### Path-following analysis for stationary solutions at Ta = 0



- symmetry breaking bifurcation, with
- an axissymmetric and an cubic symmetric state bifurcate simultaneously
- existence of unstable and stable solutions

Source: K. Bergemann, F. Feudel, C. Egbers, M. Gellert, R. Hollerbach, L. Tuckerman, *Spherical convection* - *the non-rotating situation revisited*, Topical Team meeting 11.-12. June 2009, Cotbus, unpublished presentation

Convection in low rotating spherical shells 25/42

### Global variables for *Ta* low ( $Ta \le 10^4$ )

B. Futterer and C. Egbers

#### Introduction

Motivation

Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison



Convection in low rotating spherical shells 26/42

### Global variables for *Ta* low ( $Ta \le 10^4$ )

B. Futterer and C. Egbers

Introduction

Physical Basics

simulation Borders of low

Low rotation:

Low rotation:

Summary,

Outlook and Appendices

State of the art,

Time series, linear

Parameter regimes: single images Parameter regimes: constructed images Experimental/ numerical comparison

physical basics

path-following Experimental apparatus

analysis,

transition to higher

transition to higher

rotation

Ra

Ta

3D numerical

Motivation



Convection in low rotating spherical shells 27/42

B. Futterer and C. Egbers

#### Introduction

Motivation

Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

### Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

### Experiment conditions

- GeoFlow experiment container, integrated in Fluid Science Laboratory (FSL) of COLUMBUS module on ISS
- launch: Feb 7, 2008
- start: Aug 8, 2008
- return: March 2009



Sources: European Space Agency (ESA); National Aeronautics and Space Administration (NASA); EADS Astrium GmbH, Friedrichshafen

Convection in low rotating spherical shells 28/42

B. Futterer and C. Egbers

#### Introduction

Motivation Physical Basics

3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

12

200

State of the art, physical basics

Time series, linear analysis, path-following

### Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

### Processing and data transfer from ISS to BTU



#### Convection in low rotating spherical shells 29/42

#### B. Futterer and C. Egbers

#### Introduction

Motivation

Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

### Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

### Interferometry: camera position and image view



- temperature gradient → density gradient → refractive index gradient
   → variation of optical path length → interference visualized with Wollaston shearing interferometry
- triggering of image capture each  $60^{\circ}$ 
  - ightarrow 6 positions gives measurement picture of whole hemispherical surface

### Data volume

images | 200 GB telemetry | 50 GB

telemetry - technical values, scientific values ( $\Delta T$ ,  $\mu g$ , etc.)

#### Convection in low rotating spherical shells 30/42

## B. Futterer and C. Egbers

#### Introduction

Motivation Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

### Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

### Dynamics of GeoFlow:

... with specific selection for first evaluation:  $Ta \neq 0$ 



#### Convection in low rotating spherical shells 31/42

## B. Futterer and C. Egbers

#### Introduction

Motivation

Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

### Tracking stability line





#### Convection in low rotating spherical shells 32/42

## B. Futterer and C. Egbers

#### Introduction

Motivation

Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

### Tracking stability line





#### Convection in low rotating spherical shells 33/42

## B. Futterer and C. Egbers

#### Introduction

Motivation Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

### Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

### Dynamics of GeoFlow:

... with specific selection for first evaluation: Ta = 0



Convection in low rotating spherical shells 34/42

B. Futterer and C. Egbers

#### Introduction

Motivation Physical Basics

3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

### Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

### Octahedral solution and its appearance in fringes

Pattern of convection by visualization of temperature field in radial direction with view at the top of the sphere, i.e. the middle of the image is the 'polar' region. Isolines demonstrate character of the pattern, captured by interferometry. Dark shading shows hot up-flow:

![](_page_33_Picture_17.jpeg)

#### fringe pattern

- topology at the polar region, partly outreaching to equator
- shows a repetition of patterns every second position

## Tracking stable solution

spherical shells 35/42

Convection in low rotating

B. Futterer and C. Egbers

#### Introduction

Motivation

Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

## Run#2: $\Delta T_{soll} = 2.2 \ K$ , $Ra_{centr,soll} = 3.15 \cdot 10^4$

![](_page_34_Picture_18.jpeg)

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#### Introduction

Motivation Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

### Parameter regimes: constructed images

Experimental/ numerical comparison

![](_page_35_Picture_15.jpeg)

### 1st image

![](_page_35_Picture_17.jpeg)

### 2nd image

![](_page_35_Picture_19.jpeg)

1st image -> 0°

![](_page_35_Picture_21.jpeg)

2nd image -> 60°

- image taken every  $60^{\circ} \rightarrow$  images overlap  $\rightarrow$  only a sector is visible
- defined mask (ROI) over image sequence  $\rightarrow$  6 sectors
- note: no interpolation, because of mixing fringes to gray
- note: pole is supposed to be fixed

![](_page_35_Picture_27.jpeg)

![](_page_35_Picture_28.jpeg)

![](_page_35_Picture_29.jpeg)

Convection in low rotating spherical shells 37/42

B. Futterer and C. Egbers

#### Introduction

Motivation Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

### Reconstruction of images for specific part during RUN #4

![](_page_36_Picture_16.jpeg)

#### Convection in low rotating spherical shells 38/42

## B. Futterer and C. Egbers

#### Introduction

Motivation Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

![](_page_37_Figure_15.jpeg)

### Parameter Regime with numerical and experimental data base

#### Convection in low rotating spherical shells 39/42

## B. Futterer and C. Egbers

#### Introduction

Motivation Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

### Parameter regimes: constructed images

Experimental/ numerical comparison Patterns of convection in the rapid rotation regime: Alignment of convective cells at the tangent cylinder

 $\begin{aligned} Ra_{centr} &= 8.87 \cdot 10^4 \\ Ta &= 8.59 \cdot 10^6 \end{aligned}$ 

![](_page_38_Picture_17.jpeg)

$$\begin{aligned} \textit{Ra}_{centr} &= 1.17 \cdot 10^5 \\ \textit{Ta} &= 1.34 \cdot 10^7 \end{aligned}$$

![](_page_38_Picture_19.jpeg)

'columnar cells'

Convection in low rotating spherical shells 40/42

#### B. Futterer and C. Egbers

#### Introduction

Motivation Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

### Patterns of convection in the moderate rotation regime: Increase of thermal forcing leads to symmetry breaking bifurcations

 $Ra_{centr} = 3.15 \cdot 10^4$  $Ta = 8.59 \cdot 10^4$ 

![](_page_39_Picture_17.jpeg)

 $\begin{aligned} \textit{Ra}_{centr} &= 6.01 \cdot 10^4 \\ \textit{Ta} &= 8.59 \cdot 10^4 \end{aligned}$ 

![](_page_39_Picture_19.jpeg)

 $\begin{aligned} \textit{Ra}_{centr} &= 8.87 \cdot 10^4 \\ \textit{Ta} &= 8.59 \cdot 10^4 \end{aligned}$ 

![](_page_39_Picture_21.jpeg)

#### Convection in low rotating spherical shells 41/42

## B. Futterer and C. Egbers

#### Introduction

Motivation Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

### Alignment for single image: Identification of fringe pattern as 'columnar cells'

![](_page_40_Picture_16.jpeg)

![](_page_40_Figure_17.jpeg)

	experimental	numerical
Ra <sub>centr</sub>	$9\cdot 10^4$	$5\cdot 10^4$
Ta	$9\cdot 10^6$	$4\cdot 10^6$

#### $\rightarrow$ shift between experimental and numerical stability regimes

Convection in low rotating spherical shells 42/42

## B. Futterer and C. Egbers

#### Introduction

Motivation

Physical Basics

## 3D numerical simulation

Borders of low rotation

Low rotation: transition to higher *Ra* 

Low rotation: transition to higher *Ta* 

#### Summary, Outlook and Appendices

State of the art, physical basics

Time series, linear analysis, path-following

Experimental apparatus

Parameter regimes: single images

Parameter regimes: constructed images

Experimental/ numerical comparison

### Summary

- GeoFlow
  - spherical Rayleigh-Bénard convection experiment in self-gravitating force field
  - microgravity environment of COLUMBUS on ISS
  - superposition of rotation
- dynamics for
  - non-rotating case
    - coexisting of several modes (axisymmetric, cubic, pentagonal)
    - influence of initial conditions to reach different stable states
    - transition from steady to irregular flow with remnant tetrahedral symmetry
  - rotating case
    - complex pattern drift
    - transition to stabilizing effects due to centrifugal forces
    - transition from steady via periodic to irregular flow
- first evaluated experimental images show numerically presumed dynamics and
  - for the non-rotating case: octahedral, stationary solution
  - for the rotating case: stability line