# Tutorial on Modern Ultra Low Noise Microwave Transistor Oscillator Design

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A typical linear oscillator phase noise model (block diagram) Leeson Model





A typical block diagram of feedback oscillator circuit



Colpitts oscillator with base-lead inductances and package capacitance.  $C_C$  is neglected. The expression of input impedance is given as

$$Z_{IN}\Big|_{pacakage} = -\left[\frac{Y_{21}}{\omega^2 (C_1 + C_p)C_2} \frac{1}{(1 + \omega^2 Y_{21}^2 L_p^2)}\right] - j\left[\frac{(C_1 + C_p + C_2)}{\omega (C_1 + C_p)C_2} - \frac{\omega Y_{21}L_p}{(1 + \omega^2 Y_{21}^2 L_p^2)} \frac{Y_{21}}{\omega (C_1 + C_p)C_2}\right]$$



#### This Figure shows the R&S vector analyzer and the test fixture





Typical measurement setup for evaluation of large signal parameters (R&S vector analyzer and the test fixture for the transistor of choice)

Agilent now calls this X Parameters



The bias, drive level, and frequency dependent S parameters are then obtained for practical use.

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Measured large-signal  $S_{11}$  of the BFP520





Measured large-signal  $S_{12}$  of the BFP520





Measured large-signal  $S_{21}$  of the BFP520





Measured large-signal  $S_{\!\scriptscriptstyle 22}$  of the BFP520



800.00 600.00 400.00 200.00 0.00 -200.00 0.00 10.00 20.00 10.00 20.00 10.00 20.00 10.00 0

Typical transient simulation of a ceramic resonator-based high-Q oscillator (node of the voltage for display is taken from the emitter)



This Figure illustrates the start and steady-state oscillation conditions.



A typical start and steady-state oscillation conditions.

 $R_a(A, f)$  is the starting negative Resistance, which gets lower as the amplitude increases.

Therefore, feedback must be sufficient to maintain enough negative resistance to sustain oscillating.



## Y<sub>21</sub> Large Signal Calculation



x = normalized drive level

$$V_1\big|_{peak} = \frac{kT}{q}x$$

 $Y_{21}\Big|_{l \operatorname{arg} e-signal} = G_m(x)$   $Y_{21}\Big|_{small-signal} = \frac{I_{dc}}{kT/q}\Big| = g_m$   $Y_{21}\Big|_{l \operatorname{arg} e-signal} = G_m(x) = \frac{qI_{dc}}{kTx}\left[\frac{2I_1(x)}{I_0(x)}\right]_{n=1} = \frac{g_m}{x}\left[\frac{2I_1(x)}{I_0(x)}\right]_{n=1}$   $\frac{[Y_{21}]_{l \operatorname{arg} e-signal}}{[Y_{21}]_{small-signal}}\Big|_{n=1} = \frac{G_m(x)}{g_m} \Rightarrow \frac{2I_1(x)}{xI_0(x)}$ 

$$|Y_{21}|_{small-signal} > |Y_{21}|_{l \arg e-signal} \implies g_m > G_m(x)$$



20.00 x=Drive-Level x=20 15.00 10.00 lc(\_lib1) [mA] x=3 5.00 0.00 -5.00 2.50 7.50 10.00 12.50 17.50 20.00 5.00 15.00 Time [nsec]

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Plot shows the collector current as a function of time with respect to normalized base drive Voltage *x*.





A typical phase noise plot of LC-based 1GHz oscillator as a function of x



#### GaAsOsc



#### DiodeOsc





A typical block diagram where oscillator acts like a mixer.



#### The resulting phase noise in linear terms can be calculated as

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This equation is the linear Leeson equation, with the pushing effect omitted and the flicker term added by Dieter Scherer (Hewlett Packard, about 1975); the final version with the pushing (supply voltage dependency VCO effect added by Rohde 2004), is

$$(f_m) = 10 \log \left\{ \left[ 1 + \frac{f_0^2}{(2f_m Q_L)^2} \right] \left( 1 + \frac{f_c}{f_m} \right) \frac{FkT}{2P_{sav}} + \frac{2kTRK_0^2}{f_m^2} \right\}$$

This pushing also applies to the VCO case.





A typical phase noise plot for an ideal 1 GHz oscillator phase noise of about – 140 dBc/Hz at offset of 10 kHz offset, assuming unloaded Q of 1 million loaded Q of 500, noise factor 6 dB, flicker frequency 1kHz, oscillator voltage gain 1Hz/V, equivalent noise resistance of tuning diode 10hm and average power at oscillator output 10 dBm. No diode contribution



## **Non-Linear Oscillator Equation**

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$$L\frac{di(t)}{dt} + (R_{L} - R_{N}(t))i(t) + \frac{1}{C}\int i(t)dt = e_{N}(t)$$

This is a nonhomogeneous differential equation, which can be simplified to [1, Ch-8, pp. 159-232]

$$L\left[-I_{1}(t)(\omega + \frac{d\varphi_{1}(t)}{dt})\sin[\omega t + \varphi_{1}(t)] + \frac{dI_{1}(t)}{dt}\cos[\omega t + \varphi_{1}(t)]\right] + \left[(R_{L} - R_{N}(t))I(t)\right] + \frac{dI_{1}(t)}{dt}\cos[\omega t + \varphi_{1}(t)] + \frac{dI_{1}(t)}{dt}\cos[\omega t + \varphi_{1}(t)]\right] + \frac{dI_{1}(t)}{dt}\cos[\omega t + \varphi_{1}(t)] + \frac{dI_{1}(t)}{$$

$$\frac{1}{C} \left\{ \left[ \frac{I_1(t)}{\omega} - \frac{I_1(t)}{\omega^2} \left( \frac{d\varphi_1(t)}{dt} \right) \right] \sin[\omega t + \varphi_1(t)] + \frac{1}{\omega^2} \left( \frac{dI_1(t)}{dt} \right) \cos[\omega t + \varphi_1(t)] \right\} = e_N(t)$$

Further

where  $\overline{R_N(t)}$  is the average **negative** resistance under large signal condition.

$$\overline{R_N(t)} = \left[\frac{2}{T_0 I}\right]_{t-T_0}^t R_N(t)I(t)\cos^2[\omega t + \varphi]dt$$



## And The SSB Phase Noise Is:

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$$f(\omega) = 10 \times \log \left[ k_0 + \left( \frac{k^3 k_1 \left[ \frac{Y_{21}^+}{Y_{11}^+} \right]^4 [y]^{4p}}{[Y_{21}^+]^6 [y]^{6q}} \right) \left( \frac{1}{(y^2 + k)} \right) \right] \left[ \frac{[1 + y]^2}{y^2} \right] \frac{Q_{\text{max}}^2}{Q_0^2}$$

Where

$$y = \frac{C_1}{C_2} \quad k_0 = \frac{kTR}{\omega^2 \omega_0^2 L^2 V_{cc}^2 C_2^2} \quad k_1 = \frac{qI_c g_m^2 + \frac{K_f I_b^{AF}}{\omega} g_m^2}{\omega^2 \omega_0^4 L^2 V_{cc}^2} \qquad k_2 = \omega_0^4 (\beta^+)^2 \qquad k = \frac{k_3}{k_2 C_2^2}$$

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First ever complete and correct large signal phase noise calculation (Rohde 2004)





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A typical 1 GHz oscillator circuit





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A CAD Simulated (Ansoft Designer) phase noise plot for 1 GHz oscillator circuit



A CAD Simulated (MATLAB) phase noise plot for 1 GHz oscillator circuit



### Multiple Magnetically Coupled Resonators

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The quality factor of the coupled resonator network previously shown is given by

$$\left[Q_{coupled}\left(\omega\right)\right]_{\omega=\omega_{0}} = \frac{\omega_{0}}{2} \left[\frac{\partial\phi}{\partial\omega}\right] \Rightarrow \frac{2Q_{0}(1+\beta)}{(1+Q_{0}^{2}\beta^{2})} \rightarrow \left[\frac{2Q_{0}(1+\beta)}{(1+Q_{0}^{2}\beta^{2})}\right]_{\beta<<1} \approx 2Q_{0}$$



Capacitive coupled 2 resonators





Circuit with Resonators





CAD simulated phase noise plot for the single resonator (1-resonator) and the identical coupled resonator (2-resonators)



Measured phase noise plots for the single resonator (1-resonator) and the identical coupled resonator (2-resonator





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Layout of the MCLR VCO (500MHz-2500MHz) (Patented)



MCPTR (Multi Coupled Planar Transmission Line Resonators) 175 150 **Optimum Operating Mode** 125 and Optimum Class of Operation **Coupled Resonator Uncoupled Resonator** 

3.5

4.5

5.5

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Measured Q of resonators (uncoupled, coupled and MCLR)

Frequency (GHz)

2.5



100

75

50

25

0.0

0.5

1.5

Q

## Noise Optimization $\frac{d}{dm} \left[ 10 \log \left\{ \left[ 1 + \frac{f_0^2}{[2f_m Q_0 m(1-m)]^2} \right] \left( 1 + \frac{f_c}{f_m} \right) \frac{FkT}{2P_0} + \frac{2kTRK_0^2}{f_m^2} \right\} \right|_{m}$ $m_{opt} \rightarrow 0.5 \Rightarrow \left[\frac{d\phi}{d\omega}\right]_{\phi=\phi_{opt}} = \frac{Q_{unloaded}}{\omega_0}$ Coupling Factor = 0.5 Collector $C_c$ Base $v_{bn}$ $C_{v|k}$ Crystal Emitter $\pm C$ $| R_n(t) | C_2$ $r_{e1} r_{e1} = r_e ||(1/Y_{21})|$ $R_{n}(t)$ : Negative Resistance **F** (Noise Factor)

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$$F = 1 + \frac{Y_{21}^+ C_2 C_c}{(C_1 + C_2)C_1} \left[ r_b + \frac{1}{2r_e} \left( r_b + \frac{(C_1 + C_2)C_1}{Y_{21}^+ C_2 C_c} \right)^2 \left( \frac{1}{\beta^+} + \frac{f^2}{f_T^2} \right) + \frac{r_e}{2} \right]$$

Noise Factor of Oscillator





Layout of 1GHz Colpitts oscillator (Ceramic resonator oscillator)





Simulated phase noise plot of for CRO





Measured phase noise plot of the CRO





Block diagram of a user-defined MCLR VCO





Layout of dual-band RCO (Patent pending)





Phase noise plot of the dual-band VCO

# Thank You





## Are there any questions?